

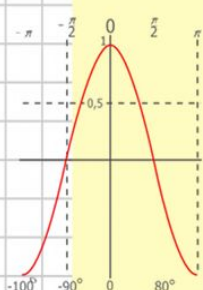
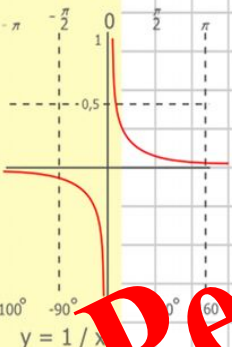
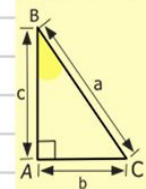
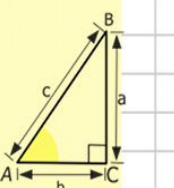
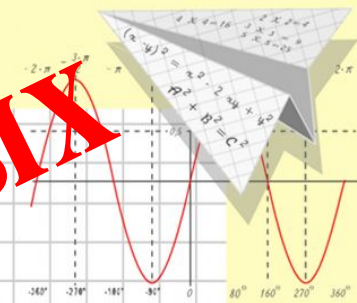
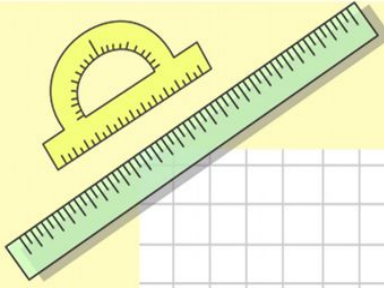
# Математик

а

**Решение показательных уравнений**

**11 класс**

**Фардиева Л. Р.**



$$\begin{array}{r} \frac{1}{2} 500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$

- 2 x 2 = 4
- 3 x 3 = 9
- 4 x 4 = 16
- 5 x 5 = 25
- 6 x 6 = 36
- 7 x 7 = 49
- 8 x 8 = 64



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

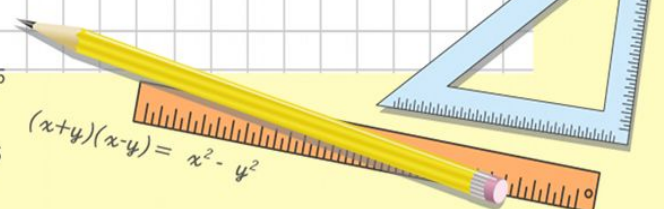
$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$



$$\sin 90^\circ = 1$$



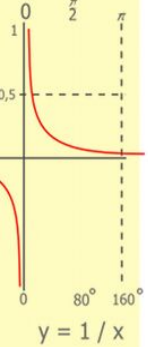
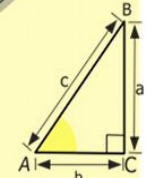
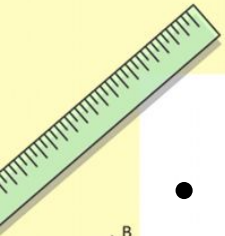
$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \\ y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$



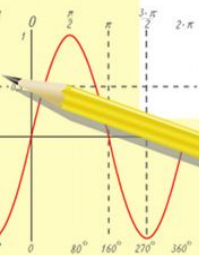
$$(x+y)(x-y) = x^2 - y^2$$

# Цели урока

- 1. Ввести понятие показательных уравнений и показать способы их решения, умение применять их при решении нестандартных задач; проверка знаний обучающихся по решению показательных уравнений;
- 2. Выработать умение мыслить, делать выводы, применять теоретические знания для решения задач; развивать самостоятельность, мышление, познавательный интерес;
- 3. Воспитание устойчивого интереса к математике, культуры поведения и общения, трудолюбия, аккуратности, положительного отношения к окружающим.



$$\begin{array}{r} \frac{1}{2} 500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$



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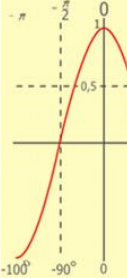
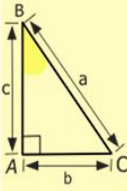
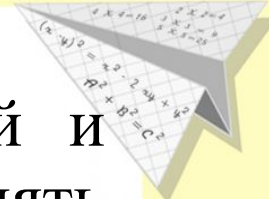


$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \end{cases}$$

$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$



$$y = \cos$$

$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



# Устная работа

Укажите, какая из данных функций является возрастающей, какая убывающей:

а)

$$y = 2^x + 3$$

б)

$$y = \left(\frac{1}{2}\right)^x - 2$$

в)

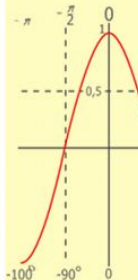
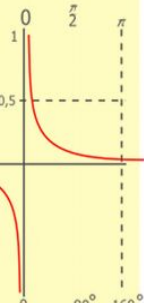
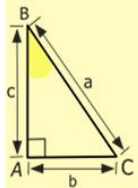
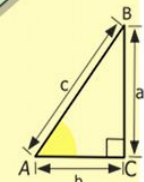
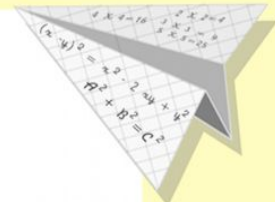
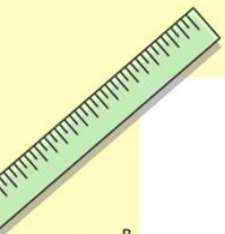
$$y = 3^x + 5$$

г)

$$y = \left(\frac{1}{7}\right)^x + 7$$

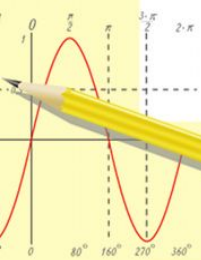
д)

$$y = 0,2^x - 4$$



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$$\sin 90^\circ = 1$$

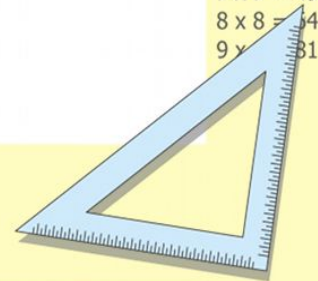


$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

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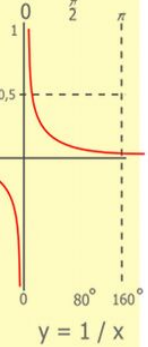
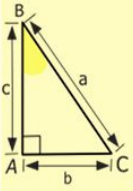
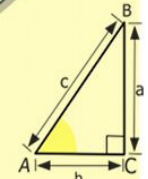
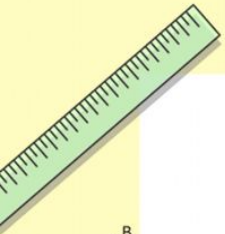
$$(x+y)(x-y) = x^2 - y^2$$



# Верно ли, что показательная функция

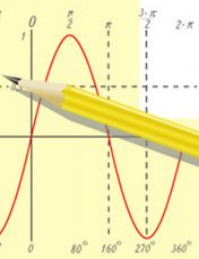
$$f(x) = a^x :$$

- а) имеет экстремумы;
- б) принимает наибольшее значение в некоторой точке  $x_0$ ;
- в) принимает в некоторой точке значение, равное нулю;
- г) является четной (нечетной)?



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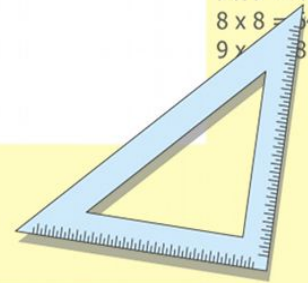


$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

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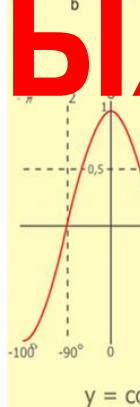
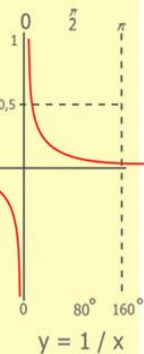
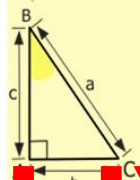
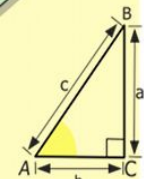
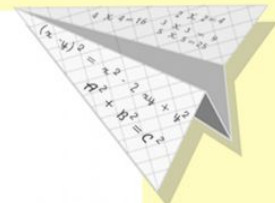
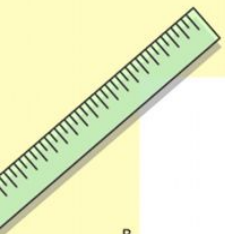
$$\frac{x}{70}$$





# Тема урока

# Решение показательных уравнений



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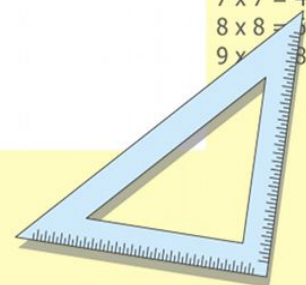
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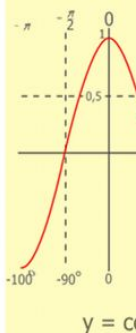
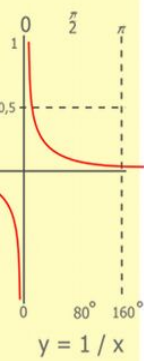
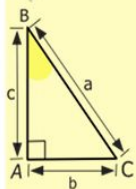
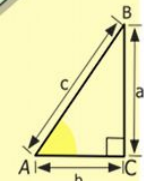
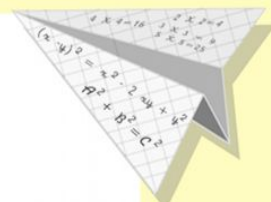
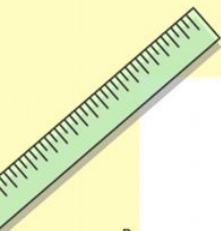


# Определение

Это уравнение, в котором неизвестные (иксы) и выражения с ними находятся в показателях каких-то степеней.

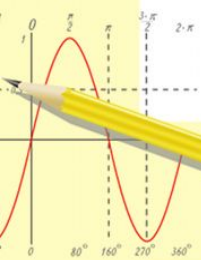
$$5^x = 25$$

$$3^{x+1} = 9$$



$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$

- $2 \times 2 = 4$
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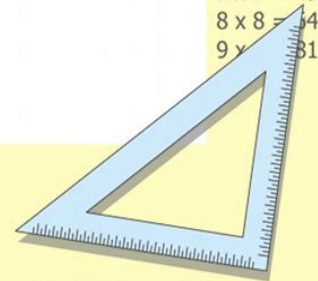
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



# Методы решения показательных уравнений:

а) Приведение к стандартному виду:

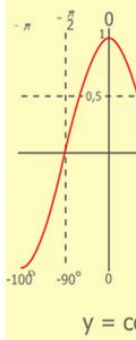
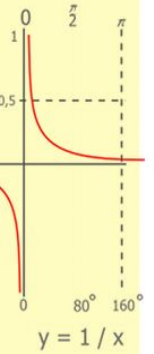
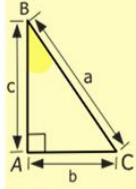
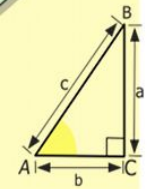
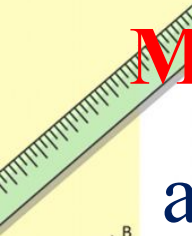
$$2^{x+3} = 16,$$

$$2^{x+3} = 2^4,$$

$$x + 3 = 4,$$

$$x = 1.$$

Ответ: 1.



$\begin{array}{r} 2500 \\ \times 42 \\ \hline 2100 \\ + 8400 \\ \hline 105000 \end{array}$

$2 \times 2 = 4$   
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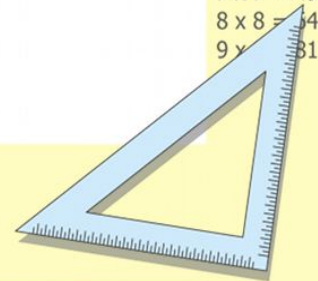
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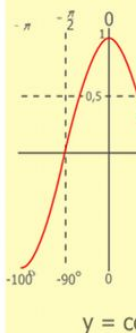
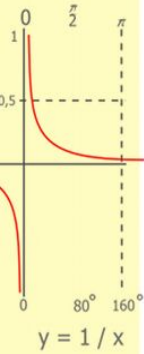
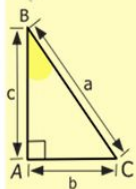
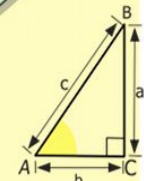
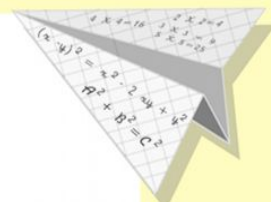
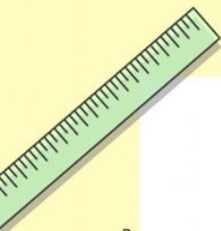


б)

$$3^x = -9$$

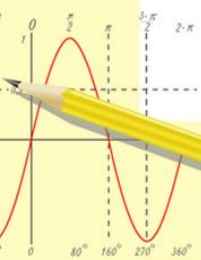
Так как показательная функция принимает только положительные значения, то данное уравнение не имеет решений.

Ответ: нет решений.



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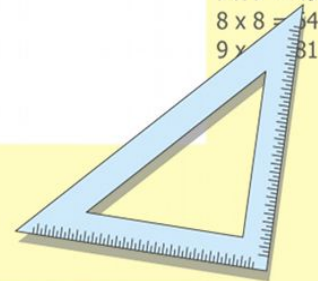
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

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$$(x+y)(x-y) = x^2 - y^2$$





в) Уравнения, решаемые с помощью вынесения общего множителя за скобки.

$$3^{x+1} - 5 \cdot 3^x + 18 = 0,$$

$$3^x \cdot 3^1 - 5 \cdot 3^x + 18 = 0,$$

$$3^x (3 - 5) + 18 = 0,$$

$$3^x (-2) + 18 = 0,$$

$$3^x = 9,$$

$$x = 2.$$

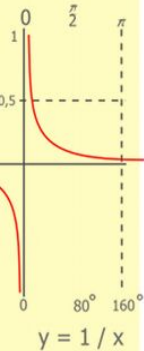
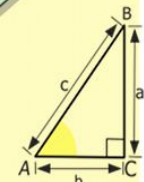
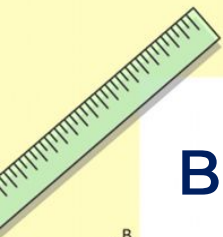
Ответ: 2

$$\begin{cases} y = \sin 90 \\ x = 25 + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \end{cases}$$

$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$



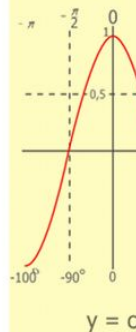
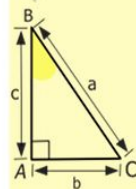
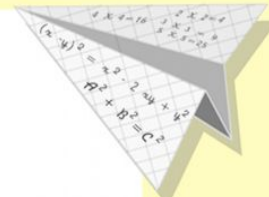
$$\begin{array}{r} \frac{1}{2} 500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$



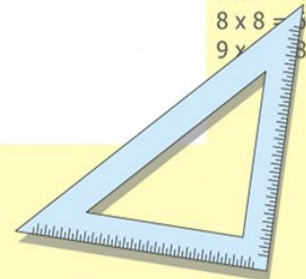
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

$$\sin 90^\circ = 1$$



$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



г) Уравнения, решаемые с помощью введения новой переменной.

$$4^x - 5 \cdot 2^x + 4 = 0,$$

$$2^{2x} - 5 \cdot 2^x + 4 = 0, \quad \text{Пусть } 2^x = y$$

$$y^2 - 5y + 4 = 0,$$

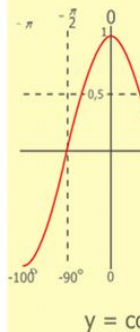
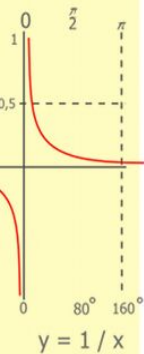
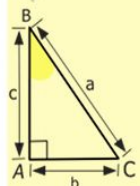
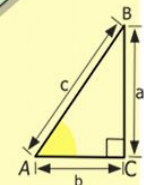
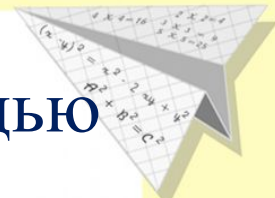
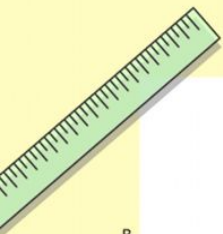
$$y_1 = 4, y_2 = 1$$

$$2^x = 4 \quad \text{или} \quad 2^x = 1$$

$$x = 2$$

$$x = 0$$

Ответ: 2; 0.



$$\begin{array}{r} 1 \ 2 \ 5 \ 00 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$

$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

$$\sin 90^\circ = 1$$

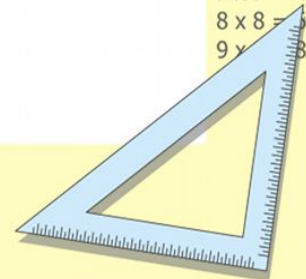


$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \end{cases}$$

$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$



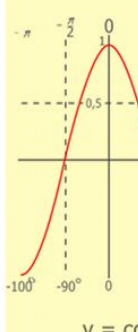
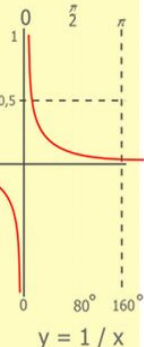
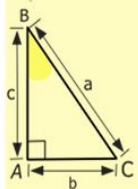
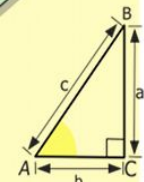
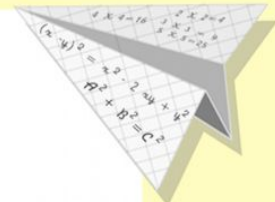
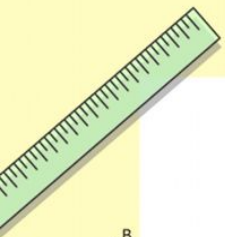
# Устная работа

Какие из следующих уравнений являются показательными:

а)  $x^2 + 4x = 0$       б)  $5^x - 25x = 0$

в)  $\sqrt{x^4} = 64$

г)  $6^y - 36^y + 216 = 0$



$\begin{array}{r} 1 \\ 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$

$2 \times 2 = 4$   
 $3 \times 3 = 9$   
 $4 \times 4 = 16$   
 $5 \times 5 = 25$   
 $6 \times 6 = 36$   
 $7 \times 7 = 49$   
 $8 \times 8 = 64$   
 $9 \times 9 = 81$



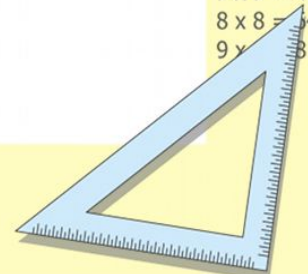
$\frac{a}{A} = \frac{b}{\sin B} = \frac{c}{\sin C}$   
 $\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$

$\sin 90^\circ = 1$



$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$   
 $\begin{cases} y = 1 \\ x = 25 + 45 \end{cases}$   
 $\frac{x}{70}$

$(x+y)(x-y) = x^2 - y^2$



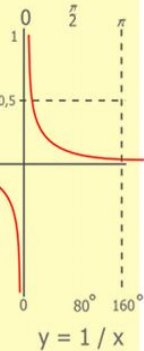
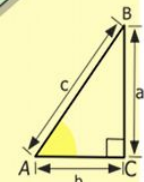
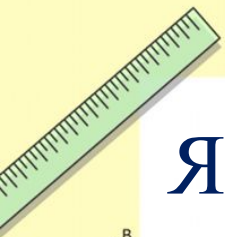
Является ли число  $x$  корнем уравнения:

а)  $2^x = 64, x = 5$

б)  $3^{x+1} = 9, x = 1$

в)  $2^x = 5^x, x = 0$

г)  $7^x = -49, x = -2$



$$\begin{array}{r} 1 \\ 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$



$$\frac{a}{A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

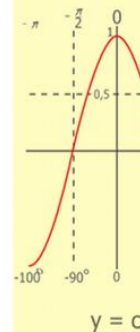
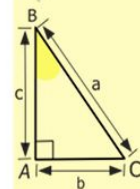
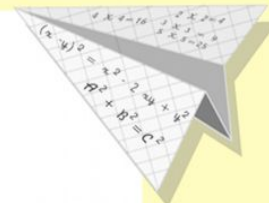
$$\sin 90^\circ = 1$$



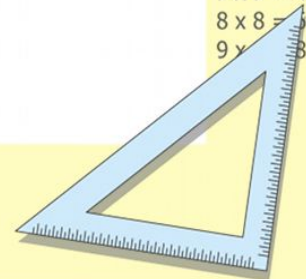
$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



$2 \times 2 = 4$   
 $3 \times 3 = 9$   
 $4 \times 4 = 16$   
 $5 \times 5 = 25$   
 $6 \times 6 = 36$   
 $7 \times 7 = 49$   
 $8 \times 8 = 64$   
 $9 \times 9 = 81$

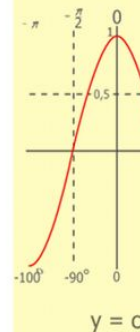
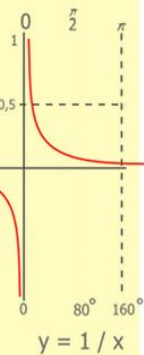
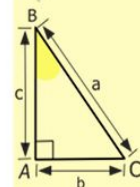
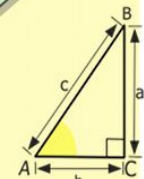
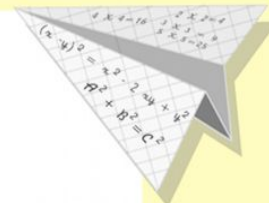
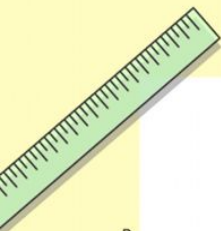


# Решение упражнений

№460 (а, в)

№463 (а, г)

№464 (в)



$$\begin{array}{r} 1 \\ 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$

$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

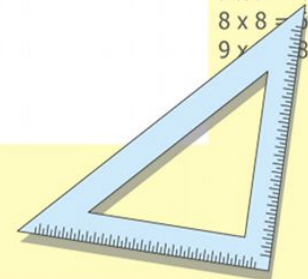
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



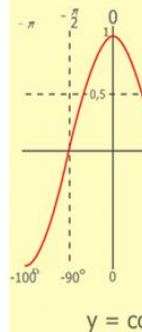
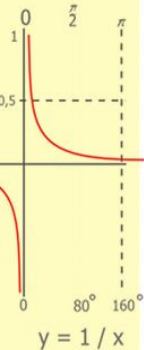
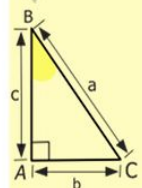
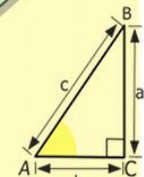
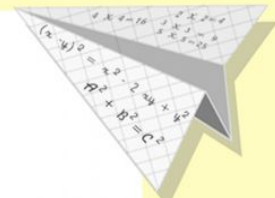
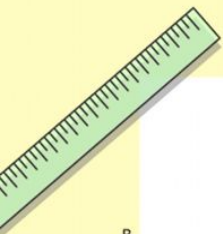


# ДОМАШНЕЕ ЗАДАНИЕ

П.36, №463(в), №464(г)

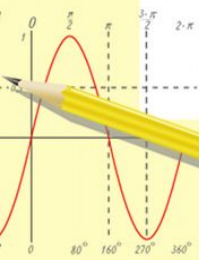
Определить, какими степенями  
и каких чисел являются числа:

2; 8; 16; 27; 32; 64; 81; 100; 125;  
128; 216; 243; 256; 343; 512; 625;  
729, 1024.



$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 2100 \\ + 8400 \\ \hline 105000 \end{array}$$

$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

$$\sin 90^\circ = 1$$

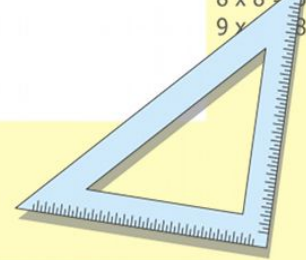


$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \end{cases}$$

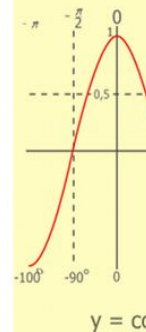
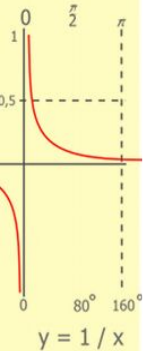
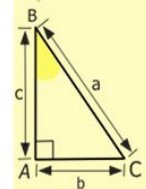
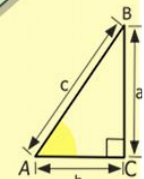
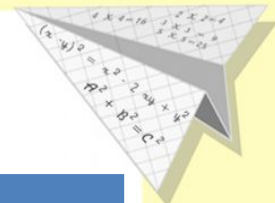
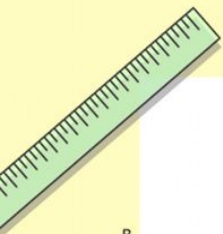
$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$



# Ответы теста:

№	1 вариант	2 вариант
1	б)	г)
2	в)	а)
3	г)	б)
4	а)	а)
5	в)	в)



$$\begin{array}{r} 1 \\ \times 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$

- 2 x 2 = 4
- 3 x 3 = 9
- 4 x 4 = 16
- 5 x 5 = 25
- 6 x 6 = 36
- 7 x 7 = 49
- 8 x 8 = 64
- 9 x 9 = 81



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

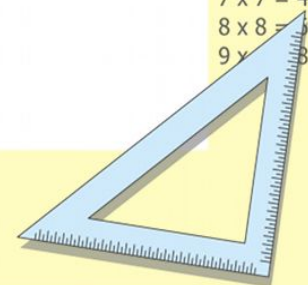
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

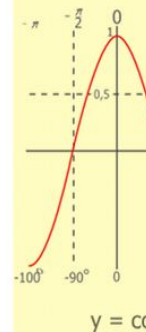
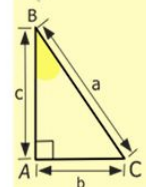
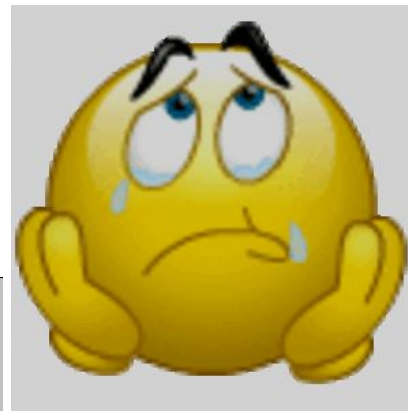
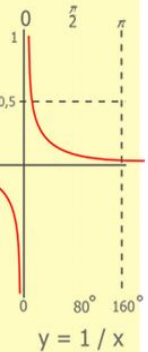
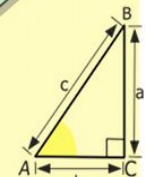
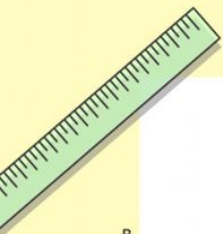
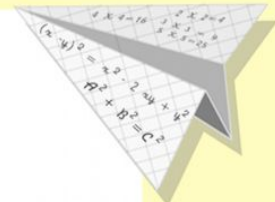
$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



# Рефлексия

## Ваше настроение



$$\begin{array}{r} 1 \\ 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$



- 2 x 2 = 4
- 3 x 3 = 9
- 4 x 4 = 16
- 5 x 5 = 25
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